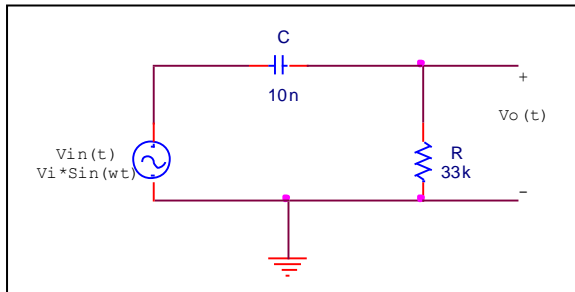


## ECE 232-Lab5

### Low-pass, High-pass and Band-pass filters

#### Preliminary Work:

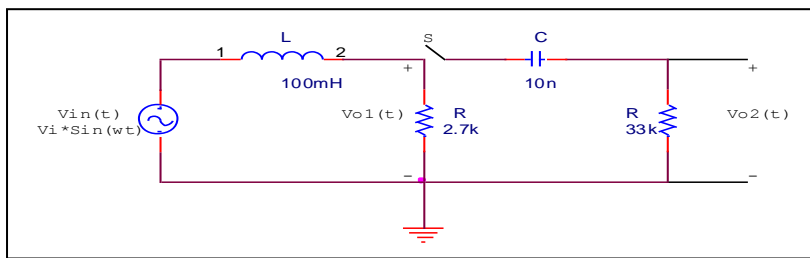
1. Consider the circuit below



Determine the frequency response function  $H(j\omega) = V_o(j\omega)/V_i(j\omega)$  and sketch the magnitude and phase characteristics (ie.

$|H(j\omega)|$  and  $\arg(H(j\omega))$  vs  $\omega$ ). Indicate the half-power frequency  $\omega_c$ , where  $|H(j\omega_c)|^2 = |H(j\omega)|_{\max}^2/2$ .

2. Consider the circuit below.



a. For S open, determine and sketch the frequency response function  $H_1(j\omega) = V_{o1}(j\omega)/V_{in}(j\omega)$ . Indicate the half-power angular frequency.

b. For S closed, determine and sketch the frequency response function  $H_2(j\omega) = V_{o2}(j\omega)/V_i(j\omega)$ . Indicate the half-power frequencies,  $\omega_{c1}$ ,  $\omega_{c2}$ , the resonant angular frequency  $\omega_0$  and the angular bandwidth  $\Delta\omega = \omega_{c2} - \omega_{c1}$ . Show that  $H_2(j\omega) \approx H_1(j\omega) * H(j\omega)$  where  $H(j\omega)$  is found in part 1, since loading is negligible.

3. Propose a method to obtain the frequency response of the circuits experimentally.

#### Experimental work:

1. Set up the circuit in part 1 of preliminary work. Plot magnitude and phase characteristics of  $|H(j\omega)|$  showing  $\omega_c$ . What is the type of this filter?
- 2.a. Set up the circuit in part 2 of preliminary work. Plot magnitude and phase characteristics of  $|H_1(j\omega)|$  showing  $\omega_c$ . What is the type of this filter?
- 2.b. Set up the circuit in part 2 of preliminary work. Plot magnitude and phase characteristics of  $|H_2(j\omega)|$  showing  $\omega_{c1}$  and  $\omega_{c2}$ . What is the type of this filter?

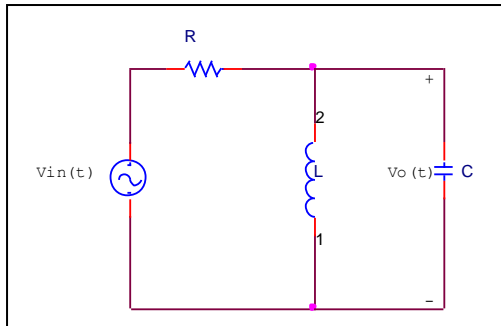
High-pass filter	YT-mode	YT-mode	XY-mode	XY-mode
$f(\text{Hz})$	$ H(j\omega) $	$\angle H(j\omega)$	$ H(j\omega) $	$\angle H(j\omega)$
$f \approx 20$				
$f = 200$				
$f = f_c$				
$f = 1000$				
$f = 5000$				

Low-pass filter	YT-mode	YT-mode	XY-mode	XY-mode
$f(\text{Hz})$	$ H(j\omega) $	$\angle H(j\omega)$	$ H(j\omega) $	$\angle H(j\omega)$
$f \approx 20$				
$f = 2000$				
$f = f_c$				
$f = 6000$				
$f = 20000$				

Band-pass filter	YT-mode	YT-mode	XY-mode	XY-mode
$f(\text{Hz})$	$ H(j\omega) $	$\angle H(j\omega)$	$ H(j\omega) $	$\angle H(j\omega)$
$f \approx 20$				
$f = 200$				
$f = f_c$				
$f = 1400 \pm 100$				
$f = 4800 \pm 100$				
$f = 20000$				

Preliminary Work: (continuation of preliminary work of lab 6)

3. Consider the circuit below,



$$L=0.1\text{H}$$

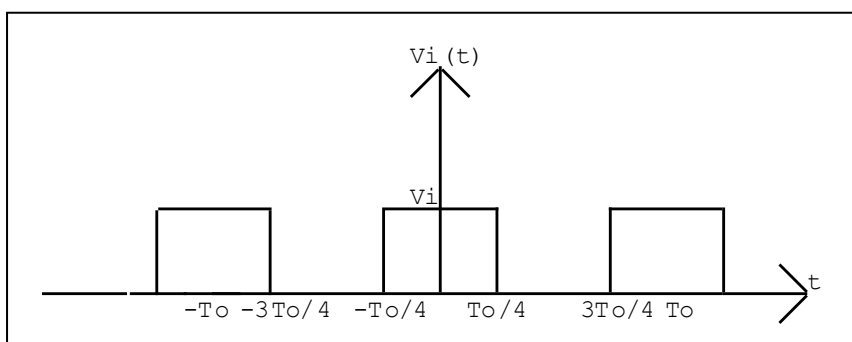
$$W_0=10\text{ krad/sec}$$

$$V_{in}(t)=V_i*\text{Sin}(\omega t)$$

- For  $R=3.3\text{k}\Omega$  find  $C$ , the bandwidth  $\Delta\omega$  and the quality factor  $Q=\omega_0/\Delta\omega$ .
- For  $R=10\text{ k}\Omega$  find  $C, Q$  and bandwidth. Determine and sketch the frequency response function  $H(j\omega)=V_o(j\omega)/V_{in}(j\omega)$ . Indicate the half-power angular frequencies and the resonant angular frequency  $\omega_0$
- A square wave of frequency  $f_0=\omega_0/2\pi$  is applied to the circuit of above circuit with element values as in part b. Since the input is periodic with period  $T_0=1/f_0$  seconds, it can be represented as a linear combination of sinusoids (Fourier series representation)

$$V_i(t)=V_i\left[\left(\frac{1}{2}\right)+\left(\frac{2}{\pi}\right)(\cos(\omega_0 t)-\left(\frac{2}{3\pi}\right)(\cos(3\omega_0 t)+\left(\frac{2}{5\pi}\right)(\cos(5\omega_0 t))\dots\right]$$

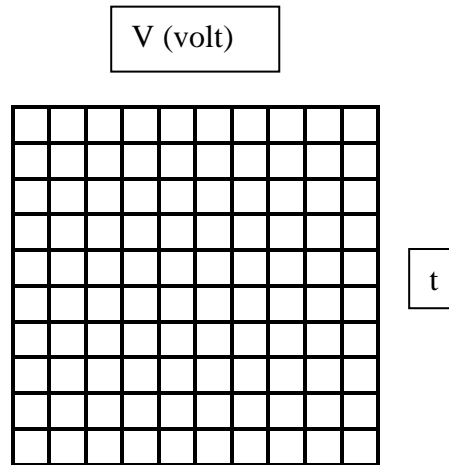
Find and sketch  $V_o(t)$ .



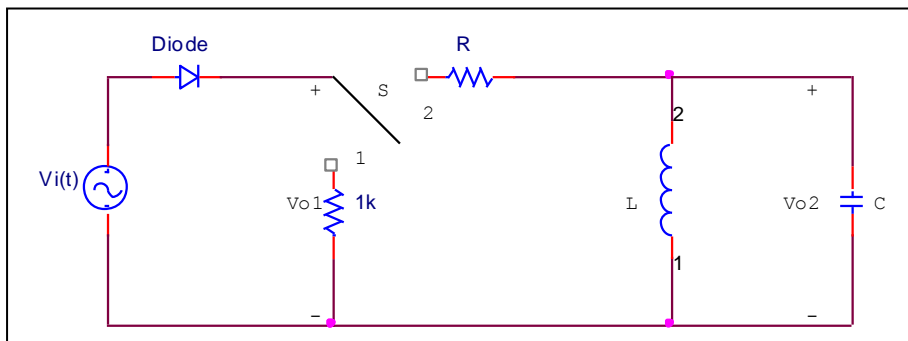
4. Comment on the filtering characteristics of the circuits considered in the preliminary work.

**Experimental Work:**

1. Set up the circuits in part 3.b of preliminary work determine and sketch the magnitude and phase characteristics of the frequency response function  $H(j\omega) = V_o(j\omega)/V_i(j\omega)$ . Find the practical  $\omega_0$  and compare it with the theoretical one.
2. Set up the circuits in part 3.c of preliminary work, Plot  $V_i(t)$  and  $V_o(t)$  together. In what way the input and the output are related. Explain.



3. Set up the circuit in figure below using the element values as in the preliminary work part 3.b.



For S in position 1 observe and plot  $V_{o1}(t)$ . For S at position 2 observe and plot  $V_{o1}(t)$  and  $V_{o2}(t)$ . Comment on the results.

$V_{o1}(t)$  V S at 1

$V_{o1}(t)$  V S at 2

$V_{o2}(t)$  V S at 2

